

Practical 1: Surveying and geodesy. Dimensions and units. Angular calculations. Using a scientific calculator for surveying calculations

Accessories to be used:

1 scientific calculator for each student

Contents:

Introduction: Surveying and Geodesy. The contents of Surveying I. and II.

- Horizontal and vertical positioning.
- Observation processing: calculations and mapping
- Setting out.

Dimensions and unit, conversions: angle, length, area.

Calculations with angles.

The application of scientific calculators for surveying calculations: angular inputs (degree, minute, second), simple trigonometric calculations. Using the memory of the calculator.

Working exercises:

Exercise 1:

Angular units (° ' " - DMS, float DMS, gradian, radian) and their conversions

$$1^\circ = 60' = 60 \times 60'' = 3600''$$

$$35^\circ 42' 15'' = 35-42-15 = 128\ 535''$$

$$35^\circ 42' 15'' = 35.704\ 167^\circ$$

$$45.351\ 947^\circ = 45^\circ 21' 07'' = 45-21-07$$

$$1\ \text{rad} = 57.295\ 780^\circ = 3\ 437.7468' = 206\ 264.8'' \approx 2 \cdot 10^5''$$

$$1'' = 0.000\ 004\ 8\ \text{rad}$$

$$5'' = 0.000\ 0242\ \text{rad}$$

$$10^\circ 32' 43'' = 10-32-43 = 0.184\ 050\ \text{rad}$$

$$1\ \text{grad (gradian)} = 1^g = 0.9^\circ$$

$$1^\circ = 1,111\ 111^g$$

$$16-43-55 = 16.731\ 944^\circ = 18.591\ 05^g$$

$$385.139\ 57^g = 346.625\ 613^\circ = 346-37-32$$

Exercise 2:

Length (km, m, cm, mm, fathom) and their conversions

$$1 \text{ km} = 1\,000 \text{ m}$$

$$0.001 \text{ km} = 1 \text{ m}$$

$$1 \text{ m} = 100 \text{ cm} = 1\,000 \text{ mm}$$

$$0.01 \text{ m} = 1 \text{ cm} = 10 \text{ mm}$$

$$0.1 \text{ cm} = 1 \text{ mm}$$

$$10.324\,51 \text{ km} = 10\,324.51 \text{ m} = 10 \text{ km } 324 \text{ m } 51 \text{ cm}$$

$$1 \text{ fathom (fth)} = 1.896\,483\,84 \text{ m}$$

$$1 \text{ m} = 0.527\,291\,6 \text{ fth}$$

$$53.14 \text{ fth} = 100.78 \text{ m}$$

$$12\,928.56 \text{ m} = 6\,817.12 \text{ fth}$$

Exercise 3:

Area (ha - hectare, m² – square meter, Hungarian acre, fth² square fathom) and their conversions

$$1 \text{ ha} = 10\,000 \text{ m}^2 = 100 \text{ m} \times 100 \text{ m}$$

$$0.0001 \text{ ha} = 1 \text{ m}^2$$

$$534\,352 \text{ m}^2 = 53.4352 \text{ ha} = 53 \text{ ha } 4352 \text{ m}^2$$

$$135 \text{ ha } 4510 \text{ m}^2 = 135.4510 \text{ ha} = 1\,354\,510 \text{ m}^2$$

$$1 \text{ fth}^2 = 3.596\,650\,955 \text{ m}^2$$

$$1 \text{ m}^2 = 0.278\,036\,432 \text{ fth}^2$$

$$200 \text{ fth}^2 = 719.330\,191\,1 \text{ m}^2 \approx 719 \text{ m}^2$$

$$1000 \text{ m}^2 = 278.036\,432 \text{ fth}^2 \approx 278 \text{ fth}^2$$

$$1 \text{ Hungarian acre (ac)} = 1600 \text{ fth}^2$$

$$1 \text{ fth}^2 = 0.000\,625 \text{ ac}$$

$$10\,324 \text{ ac} = 16\,518\,400 \text{ fth}^2$$

$$5\,415 \text{ fth}^2 = 3.384 \text{ ac}$$

$$1 \text{ ac} = 5\,754.64 \text{ m}^2 = 0.575\,464 \text{ ha}$$

$$10\ 324\ \text{ac} = 5\ 941.0903\ \text{ha} = 59\ 410\ 903\ \text{m}^2$$

$$32\ \text{ac} = 1500\ \text{fth}^2 = 52\ 700\ \text{fth}^2 = 189\ 544\ \text{m}^2 = 18\ \text{ha} = 9\ 544\ \text{m}^2 = 18.954\ 4\ \text{ha}$$

$$1\ \text{ha} = 2\ 780.4\ \text{fth}^2 = 1,737\ 75\ \text{ac} = 1\ \text{ac} = 1\ 180.4\ \text{fth}^2$$

Exercise 4:

Adding angles:

$$\gamma = \alpha + \beta \quad \text{when } \gamma > 360^\circ \text{ then } 360^\circ \text{ must be subtracted!}$$

$$\begin{array}{r} \alpha = 214-21-54 \\ +\beta = 135-44-12 \\ \hline \gamma = \mathbf{350-06-06} \end{array}$$

$$\begin{array}{r} \alpha = 314-24-41 \\ +\beta = 222-11-42 \\ \hline \gamma = \mathbf{536-36-23} \text{ } (-360^\circ) = \mathbf{176-36-23} \end{array}$$

$$\begin{array}{r} \alpha = 180-00-01 \\ +\beta = 180-00-00 \\ \hline \gamma = \mathbf{360-00-01} \text{ } (-360^\circ) = \mathbf{0-00-01} \end{array}$$

$$\begin{array}{r} \alpha = 145-25-45 \\ +\beta = 122-57-54 \\ \hline \gamma = \mathbf{268-23-39} \end{array}$$

Exercise 5:

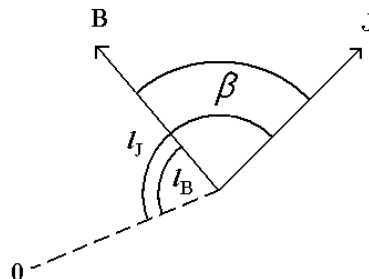
Computation of deflection angles (subtracting angles):

$$\beta = l_J - l_B \quad \text{When } \beta < 0^\circ \text{ (negative), } 360^\circ \text{ must be added to the result.}$$

$$\begin{array}{r} l_J = 214-21-54 \\ -l_B = 135-44-12 \\ \hline \beta = \mathbf{78-37-42} \end{array}$$

$$\begin{array}{r} l_J = 0-00-00 \text{ } (+360^\circ) \\ -l_B = 184-54-11 \\ \hline \beta = \mathbf{175-05-49} \end{array}$$

$$\begin{array}{r} l_J = 331-43-18 \text{ } (+360^\circ) \\ -l_B = 331-43-19 \\ \hline \beta = \mathbf{359-59-59} \end{array}$$



$$L_I = 98-22-32$$

$$\underline{-L_B = 211-55-49}$$

$$\beta = -(113-33-17) + 360^\circ = 246-26-43$$

Exercise 6:

Simple trigonometric calculations:

$$c = 43.58 \text{ m}$$

$$\alpha = 22-45-34$$

$$b = c \cos \alpha = 43.58 \cos 22-45-34 = \mathbf{40.19 \text{ m}}$$

$$c = 43.58 \text{ m}$$

$$\alpha = 22-45-34$$

$$a = c \sin \alpha = 43.58 \sin 22-45-34 = \mathbf{16.86 \text{ m}}$$

$$a = 16.86 \text{ m}$$

$$b = 40.19 \text{ m}$$

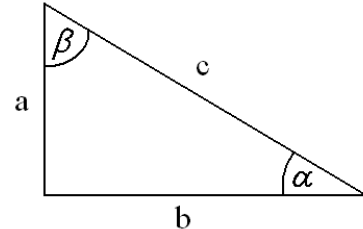
$$c = \sqrt{(a^2 + b^2)} = \sqrt{(16.86^2 + 40.19^2)} = \mathbf{43.58 \text{ m}}$$

$$\beta = \arccos (a/c) = \arccos (16.86/43.58) = \mathbf{67-14-23}$$

$$\beta = \arctan (b/a) = \arctan (40.19/16.86) = \mathbf{67-14-30}$$

$$\beta = 180^\circ - (90^\circ + 22-45-34) = \mathbf{67-14-26}$$

Why do the three calculated β values differ from each other?



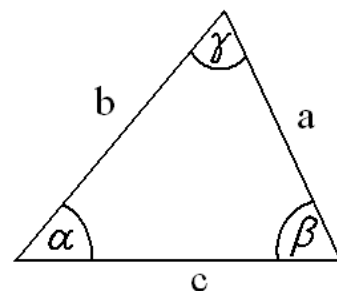
Exercise 7:

Trigonometric calculations (law of sines and cosines):

$$\alpha = 40-05-49$$

$$\beta = 67-14-16$$

$$\gamma = 180^\circ - (\alpha + \beta) = 180^\circ - (40-05-49 + 67-14-16) = \mathbf{72-39-55}$$



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$$c = 19.17 \text{ m}$$

$$a = c \sin \alpha / \sin \gamma = 19.17 \sin 40-05-49 / \sin 72-39-55 = \mathbf{12.93 \text{ m}}$$

$$b = c \sin \beta / \sin \gamma = 19.17 \sin 67-14-16 / \sin 72-39-55 = \mathbf{18.52 \text{ m}}$$

$$\begin{aligned} a &= \sqrt{(c^2 + b^2 - 2 c b \cos \alpha)} = \\ &= \sqrt{(19.17^2 + 18.52^2 - 2 \times 19.17 \times 18.52 \times \cos 40-05-49)} = \mathbf{12.93 \text{ m}} \end{aligned}$$

$$\begin{aligned} b &= \sqrt{(c^2 + a^2 - 2 c a \cos \beta)} = \\ &= \sqrt{(19.17^2 + 12.93^2 - 2 \times 19.17 \times 12.93 \times \cos 67-14-16)} = \mathbf{18.52 \text{ m}} \end{aligned}$$